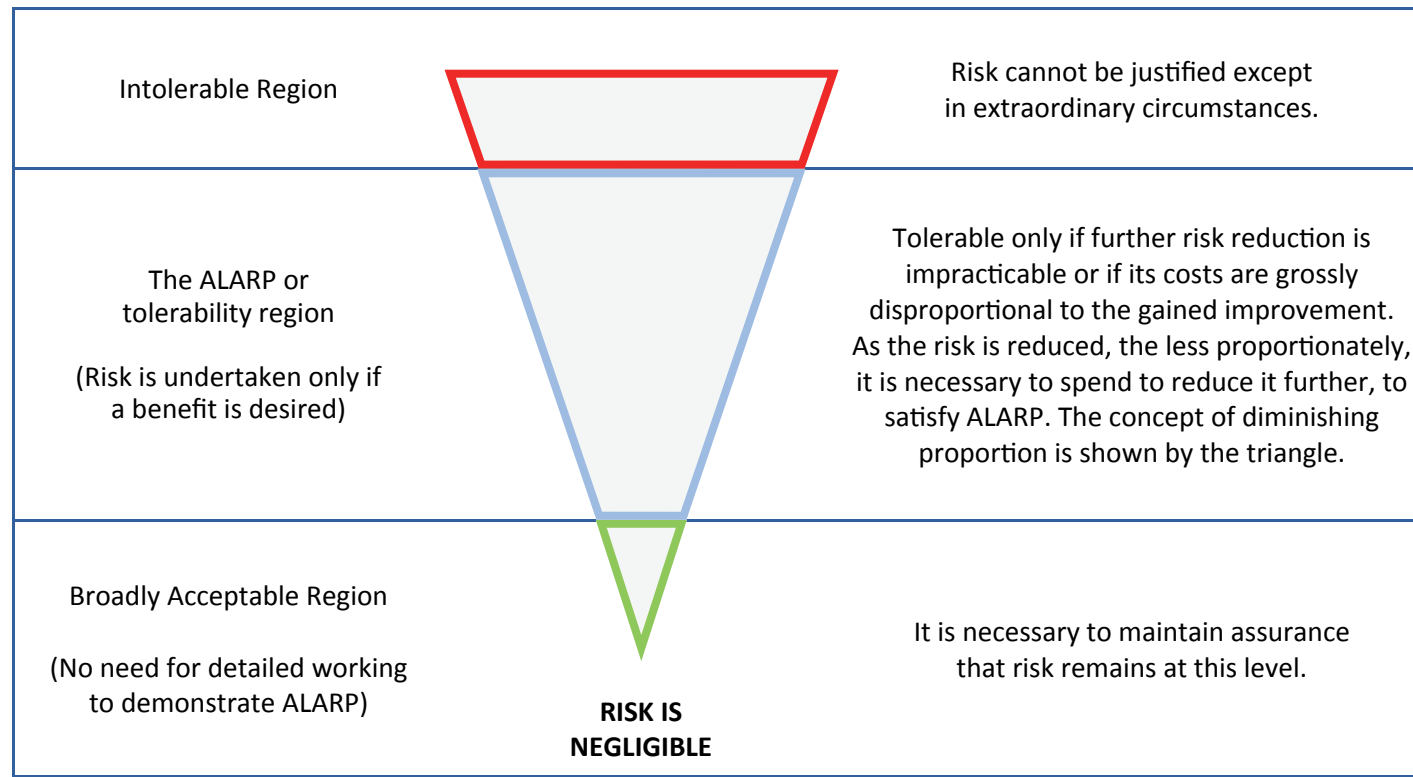
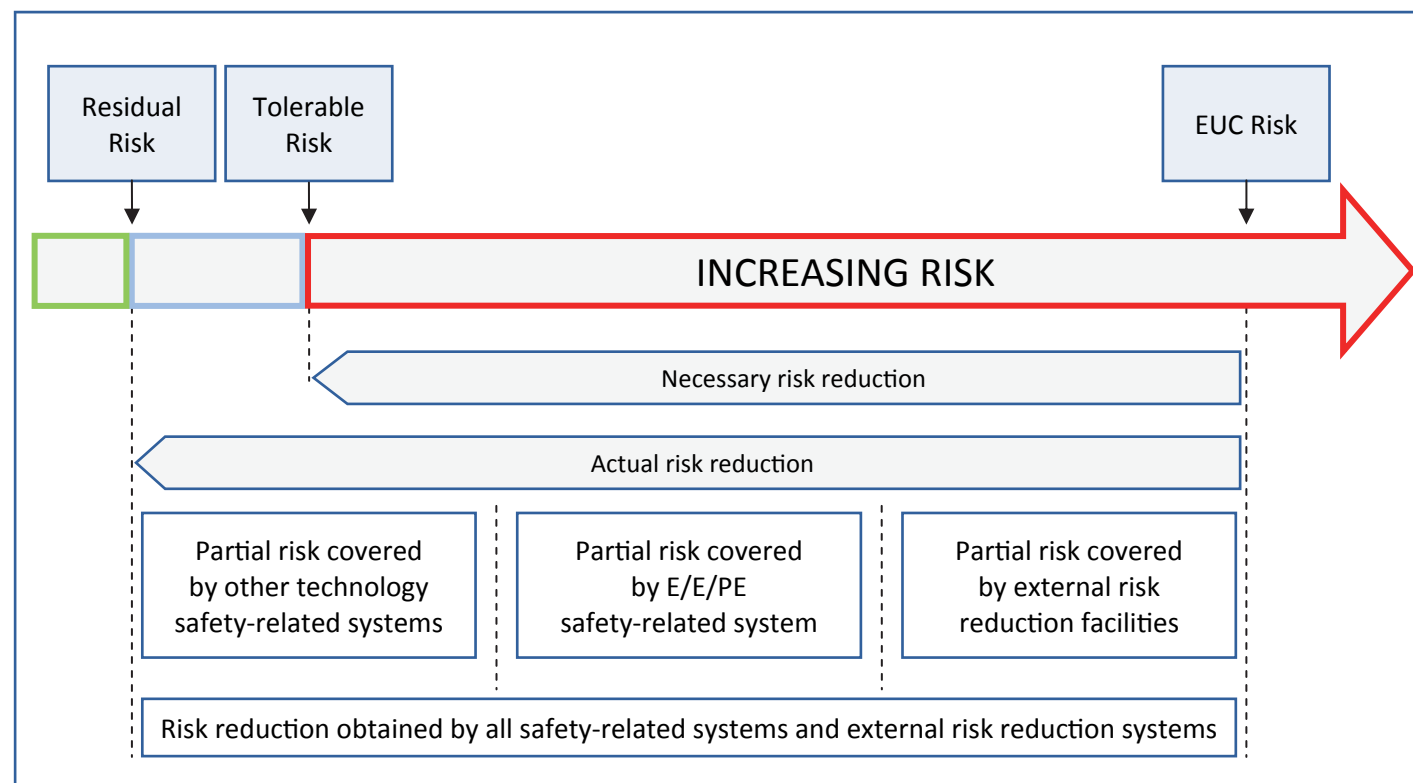


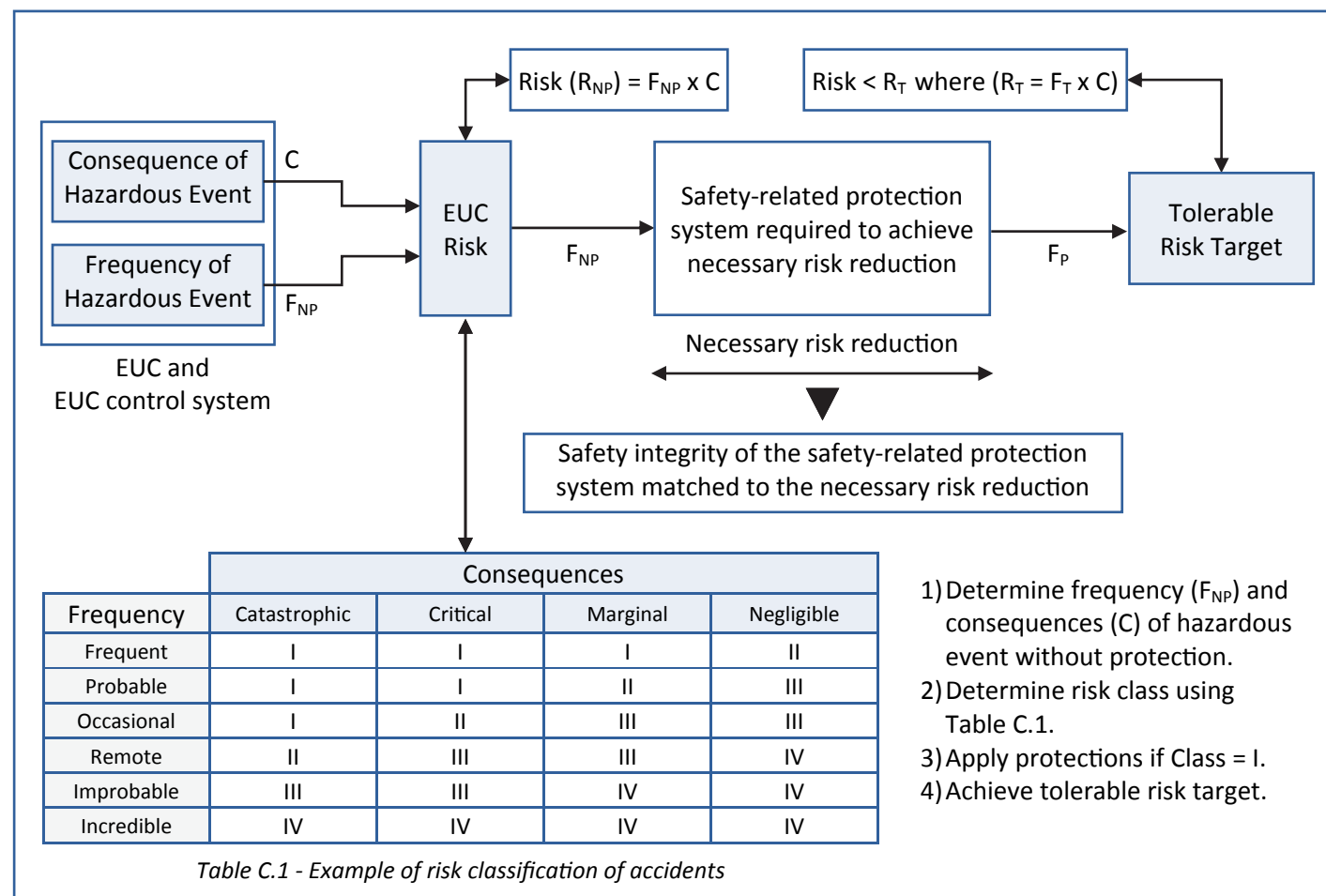
TOLERABLE RISKS AND ALARP (IEC 61508-5 ANNEX 'C')



RISK REDUCTION (IEC 61508-5 ANNEX 'A')



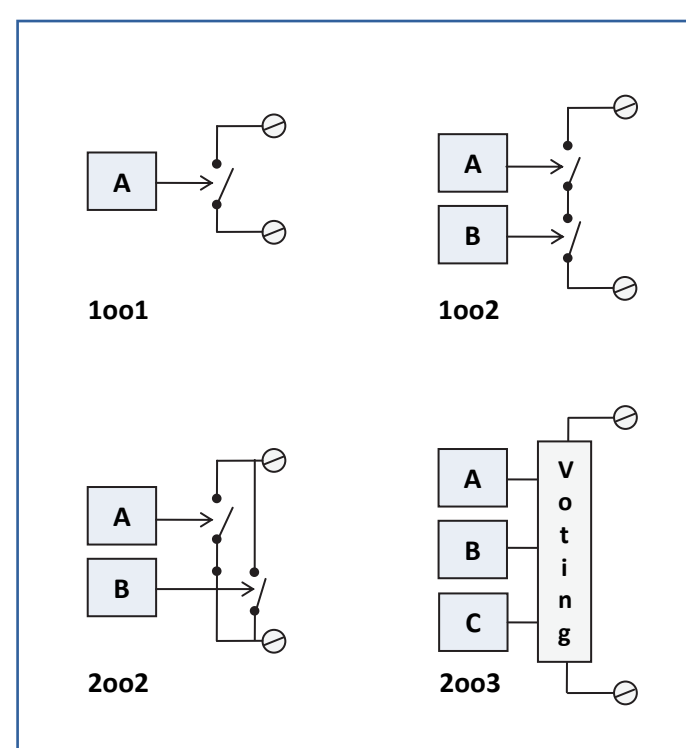
SAFETY INTEGRITY LEVEL CALCULATION (IEC 61508-5 ANNEX 'D')



MEAN TIME TO SPURIOUS FAILURE

MTTFs	
1001	$\frac{1}{\lambda_S}$
1002	$\frac{1}{2\lambda_S}$
2002	$\frac{1}{2\lambda_S^2 \times MTTR}$
2003	$\frac{1}{6\lambda_S^2 \times MTTR}$

SYSTEM ARCHITECTURES



SIL LEVELS ACCORDING IEC 61508 / IEC 61511

SIL Safety Integrity Level	PFDavg Average probability of failure on demand per year (low demand mode)	RRF Risk Reduction Factor	PFDavg Average probability of failure on demand per hour (high demand or continuous mode)
SIL 4	$\geq 10^{-5}$ and $< 10^{-4}$	100000 to 10000	$\geq 10^{-9}$ and $< 10^{-8}$
SIL 3	$\geq 10^{-4}$ and $< 10^{-3}$	10000 to 1000	$\geq 10^{-8}$ and $< 10^{-7}$
SIL 2	$\geq 10^{-3}$ and $< 10^{-2}$	1000 to 100	$\geq 10^{-7}$ and $< 10^{-6}$
SIL 1	$\geq 10^{-2}$ and $< 10^{-1}$	100 to 10	$\geq 10^{-6}$ and $< 10^{-5}$

AVERAGE PROBABILITY OF FAILURE ON DEMAND

PFDavg

Tolerable accident frequency = $\frac{1}{\text{Frequency of accidents without protections} \times \text{RRF}}$

Simplified equations

	Without common causes	With common causes (Beta factor)
1001	$\lambda_{DU} \times \frac{TI}{2}$	-
1002 1002D	$\lambda_{DU1} \times \lambda_{DU2} \times \frac{TI^2}{3}$	$\frac{[(1-\beta) \times (\lambda_{DU} \times TI)]^2 + (\beta \times \lambda_{DU} \times TI)}{3}$
1003	$\lambda_{DU1} \times \lambda_{DU2} \times \lambda_{DU3} \times \frac{TI^3}{4}$	$\frac{[(1-\beta) \times (\lambda_{DU} \times TI)]^3 + (\beta \times \lambda_{DU} \times TI)}{4}$
2002	$(\lambda_{DU1} + \lambda_{DU2}) \times \frac{TI}{2}$	$[(1-\beta) \times (\lambda_{DU} \times TI)] + \frac{(\beta \times \lambda_{DU} \times TI)}{2}$
2003	$\left[(\lambda_{DU1} \times \lambda_{DU2}) + (\lambda_{DU1} \times \lambda_{DU3}) + (\lambda_{DU2} \times \lambda_{DU3}) \right] \times \frac{TI^2}{3}$	$[(1-\beta) \times (\lambda_{DU} \times TI)]^2 + \frac{(\beta \times \lambda_{DU} \times TI)}{2}$
1001 (Et ≠ 100%)	$\lambda_{DU} \left[\left(Et \times \frac{TI}{2} \right) + (1-Et) \frac{SL}{2} \right]$	TI: Proof Test Time Interval Et: Test Effectiveness λ_{DU} : Dangerous Undetected Failures

SAFE FAILURE FRACTION (IEC 61508-2 CLAUSE 7.4)

SFF

$$\frac{\sum \lambda_{DD} + \sum \lambda_{SD} + \sum \lambda_{SU}}{\sum \lambda_{DD} + \sum \lambda_{DU} + \sum \lambda_{SD} + \sum \lambda_{SU}} = 1 - \frac{\sum \lambda_{DU}}{\sum \lambda_{TOT}}$$

	Hardware Fault Tolerance 0	Hardware Fault Tolerance 1	Hardware Fault Tolerance 2
TYPE A Components Simple devices with well-known failure modes and a solid history of operation	< 60 %	SIL 1	SIL 2
	60 % - < 90 %	SIL 2	SIL 3
	90 % - < 99 %	SIL 3	SIL 4
	> 99 %	SIL 3	SIL 4
TYPE B Components Complex components with potentially unknown failure modes	< 60 %	Not allowed	SIL 1
	60 % - < 90 %	SIL 1	SIL 2
	90 % - < 99 %	SIL 2	SIL 3
	> 99 %	SIL 3	SIL 4

Failure rate categories: λ_{DD} : Dangerous Detected; λ_{SD} : Safe Detected; λ_{DU} : Dangerous Undetected; λ_{SU} : Safe Undetected.

AVAILABILITY AND RELIABILITY

Basic Concepts:

Failure Rate: $\lambda = \frac{\text{Failures per unit time}}{\text{Components exposed to functional failure}}$

1 FIT = 1×10^{-9} Failures per hour

$MTBF = MTTF + MTTR$ $\mu = \frac{1}{MTTR}$

$MTTF = MTBF - MTTR = \frac{1}{\lambda}$ $\lambda = \frac{1}{MTTF}$

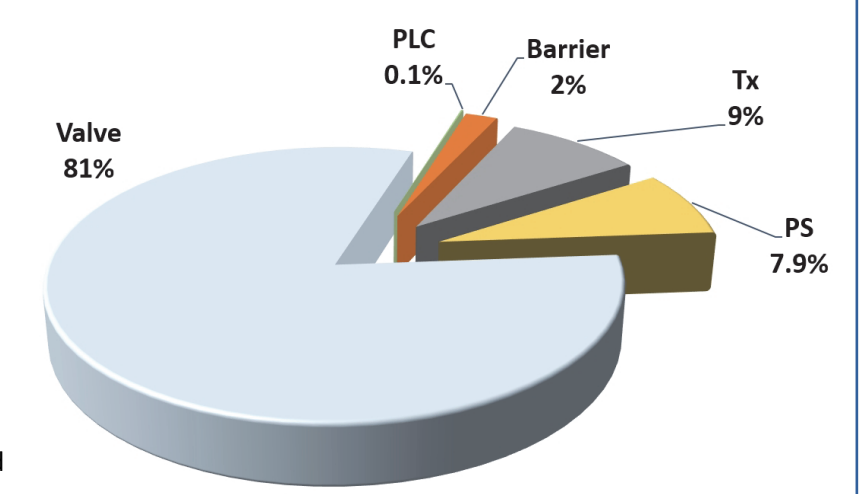
Availability = $\frac{\text{Operating Time}}{\text{Operating Time} + \text{Repair Time}} = \frac{MTTF}{MTTF + MTTR} = \frac{\mu}{\mu + \lambda}$

Unavailability = $1 - \text{Availability} = \frac{\lambda}{\mu + \lambda}$

Acronyms:
MTBF: Mean Time Between Failures
MTTF: Mean Time To Failure
MTTR: Mean Time To Repair
MTBM: Mean Time Between Maintenance
MSD: Expected Mean System Downtime
 λ : Failure rate
 μ : Repair rate

A PRACTICAL APPLICATION

Calculate MTBF, MTBFs, PFDavg, RRF, and possible SIL level of the following SIF, which includes a transmitter, a barrier, a safety PLC, and a valve as final element, in 1001 architecture. T-proof test is carried out once a year with 100% effectiveness.



The pie chart on the right shows percentages of the single sub-systems on the total PFD of the Safety Function.

The table below contains failure data provided by the manufacturer of each sub-system. Formulae to calculate requested values are indicated in the header.

Sub-system	λ_S per year	λ_{DD} per year	λ_{DU} per year	λ per year = $1/MTBF$	MTBF (yrs)	MTBFs = $1/\lambda_S$ (yrs)	PFDavg 1001 = $\lambda_{DU}/2$	% of Total PFDavg	RRF = $1/PFDavg$	SFF	SIL Level
Tx	0.00800	0.0010	0.00080	0.00980	102	125	0.000400	9 %	-	91.8 %	SIL 2
Barrier	0.00159	0.0014	0.00019	0.00318	314	629	0.000095	2 %	-	94.0 %	SIL 3
PLC	0.00135	0.0001	0.00001	0.00146	685	741	0.000005	0.1 %	-	99.3 %	SIL 3
Valve	0.01370	0.0066	0.00720	0.02750	36	73	0.003602	81 %	-	73.8 %	SIL 2
Power Supply	0.00530	0.0000	0.00070	0.00600	167	189	0.000350	7.9 %	-	88.3 %	SIL 3
Total (SIF)	0.02994	0.0091	0.00890	0.04794	21	33	0.004452	100 %	225	-	SIL 2

INFLUENCE OF PERIODIC TEST DURATION AND EFFECTIVENESS ON PFDavg (1001)

MANUAL PERIODIC TEST DURATION

The duration of a manual proof test can have a significant impact on the overall SIS performance. In 1001 architectures, during the test, the system must be taken offline, and its availability is zero. The original simplified formula is modified into:

$$PFDavg = \lambda_{DU} \times \frac{TI + TD}{TI}$$

where TI is the proof test interval and TD the test duration.

Note: The average probability of failure is strictly related to test interval (TI); increasing time between tests directly leads to higher probability of failures and therefore lower SIL levels.

Example:

$\lambda_{DU} = 0.002$ / yr; TI = 1 yr (= 8760 hrs); TD = 8 hrs
We obtain: PFDavg = $0.001 + 0.0009 = 0.0019$; RRF = $1/0.0019 = 526$ (suitable for SIL 2 level)

MANUAL PERIODIC TEST EFFECTIVENESS

The effectiveness of a periodic proof test indicates the percentage of dangerous failures detected by the test. If effectiveness is lower than 100%, the proof test does not bring the probability of failure of the system back to zero ("as new"), therefore PFDavg progressively increases in time. In this case the system not always maintains the original SIL level throughout its lifetime. The formula for calculating PFDavg when effectiveness is lower than 100% is:

$$PFDavg = (Et \times \lambda_{DU} \times \frac{TI}{2}) + [(1-Et) \times \lambda_{DU} \times \frac{SL}{2}]$$

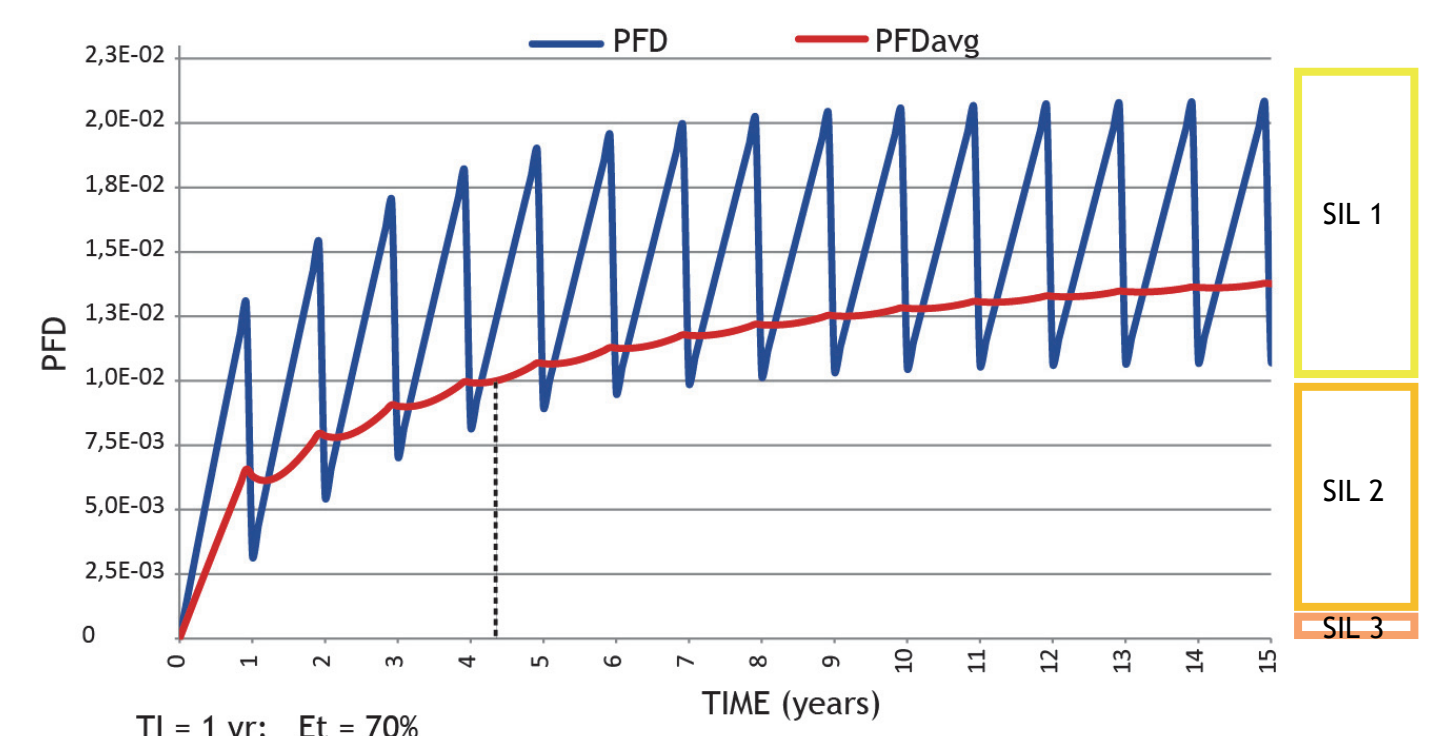
where:

Et: periodic test effectiveness to reveal dangerous failures (e.g. 90%)
SL: system lifetime. It is equal to the time until the system is completely tested (100%) or replaced. If this never happens, SL is equal to the lifetime of the whole plant.

The complete formula for calculating PFDavg taking both influences into account is:

$$PFDavg = (Et \times \lambda_{DU} \times \frac{TI + TD}{2}) + [(1-Et) \times \lambda_{DU} \times \frac{SL}{2}]$$

The following graph shows an example of PFD and PFDavg variations in case T-proof test is carried out once a year with 70% effectiveness: SIL 2 level is maintained only for about 4 years; the SIF then downgrades to SIL 1.



When dealing with SIFs, safety engineers should pay special attention to the selection of sub-systems, the time interval between periodic tests and the system architecture. A wise choice of these three key elements is what it takes to achieve the required SIL level. For more details on any of the subjects in this poster, refer to "Safety Instrumented Systems" manual by G.M. International.